Math 233: Test 2A Spring 2014 Instructor: Linda Green

Name:		
	1.	Calculators are allowed and a formula sheet ar allowed.
	2.	You must show work for full and partial credit, except where otherwise noted.
	3.	Give exact values instead of decimal approximations, except where otherwise noted.
	4.	Sign the honor pledge after completing the exam. I have neither given nor received unauthorized help on this exam.

1. (10 pts) Find the equation of the tangent plane to the surface

$$x^2y = z^2 - 7$$

at the point (1, 2, 3).

2. (10 pts) Suppose $z = \frac{x}{y}$, $x = r + s \cos t$, $y = r + s \sin t$. Find $\frac{\partial z}{\partial t}$ when r = 1, s = 2, and t = 0.

- 3. (12 pts total) Consider the function $f(x, y) = \ln(3 + xy^2)$.
 - (a) Find the directional derivative of f at the point (2,3) in the direction towards the point (1,5). (Note: you are not given a direction vector, only the first and last point of a direction vector!)
 - (b) At the point (2,3), in what direction does f increase most rapidly?
 - (c) What is the maximal rate of increase at the point (2, 3)?
 - (d) Find a unit tangent vector \vec{w} for which $D_{\vec{w}}f(2,3) = 0$.

4. (12 pts) True or false. True means always true. False means sometimes or always false. NO WORK NEEDED.

Assume that f is defined on all of \mathbb{R}^2 with continuous first and second partial derivatives.

(a) **T F** If (5,7) is a critical point of f(x,y) and $f_{xx}(5,7) > 0$ and $f_{yy}(5,7) < 0$, then f has a saddle point at (5,7).

(b) **T F** If $\nabla f(1,2) = 0$, then f has either a local minimum, a local maximum, or a saddle point at (1,2).

(c) **T F** If $\nabla f(x, y) = P(x, y)\vec{i} + Q(x, y)\vec{j}$, then $P_y(x, y) = Q_x(x, y)$.

(d) **T F** If $\lim_{x \to 0} f(x, 0) = 1$ and $\lim_{y \to 0} f(0, y) = 1$, then $\lim_{(x,y) \to (0,0)} f(x,y) = 1$.

(e) T F $\int_{2}^{4} \int_{1}^{6} x^{2} e^{xy^{3}} dy dx = 0$

(f) **T F** If $\vec{r}(t)$ is a reparametrization of $\vec{q}(u)$ such that $\vec{r}(t) = \vec{q}(2t)$, then the curvature of \vec{r} at t = 0 is 4 times the curvature of \vec{q} at u = 0.

CHOOSE YOUR ADVENTURE: Pick one of the following two problems. Please specify which problem you want graded.

- 5. (10 pts) Suppose you want to find the point(s) on the surface 3xyz = 1 that is / are closest to the origin, using the method of Lagrange multipliers. SET UP the four equations you would need to solve. (You DO NOT need to solve the equations or finish the problem!)

 OR
- 6. (10 pts) Find the absolute maximum and absolute minimum of the function $f(x, y) = 3x^2 2y^2 4y$ on the region bounded by the curves $y = x^2$ and y = 3.